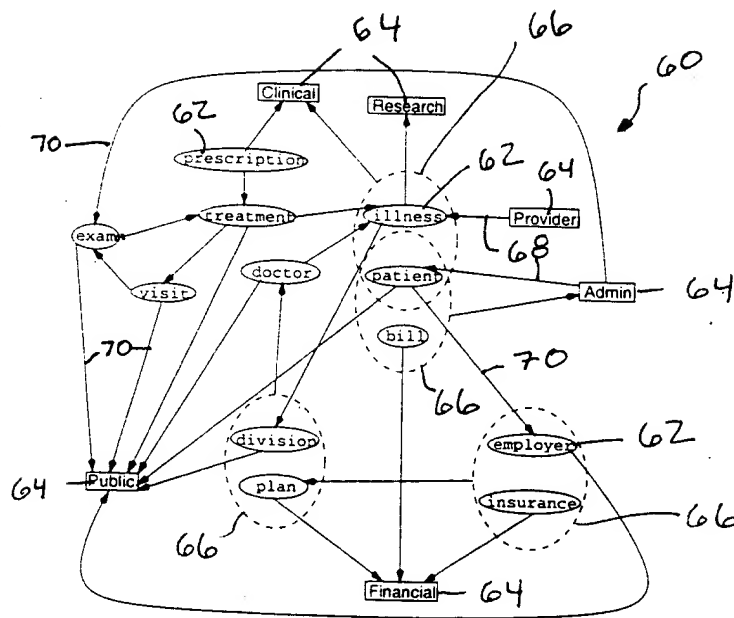


(a) A 3D lattice diagram representing a security model. The top node is labeled $\langle TS, \{ \text{Army, Nuclear} \} \rangle$. The middle layer has three nodes: $\langle TS, \{ \text{Army} \} \rangle$, $\langle S, \{ \text{Army, Nuclear} \} \rangle$, and $\langle TS, \{ \text{Nuclear} \} \rangle$. The bottom layer has three nodes: $\langle S, \{ \text{Army} \} \rangle$, $\langle TS, \{ \} \rangle$, and $\langle S, \{ \text{Nuclear} \} \rangle$. The bottom-most node is $\langle S, \{ \} \rangle$. A handwritten number '30' with an arrow points to the top node.

(b) A vertical hierarchy diagram. The nodes from top to bottom are: TopSecret, Secret, Confidential, and Unclassified. A handwritten number '40' with an arrow points to the TopSecret node.

(c) A diamond-shaped lattice diagram. The top node is HMO. The second layer has Admin and Provider. The third layer has Clinical. The bottom layer has Financial and Research. The bottom-most node is Public. A handwritten number '50' with an arrow points to the HMO node.



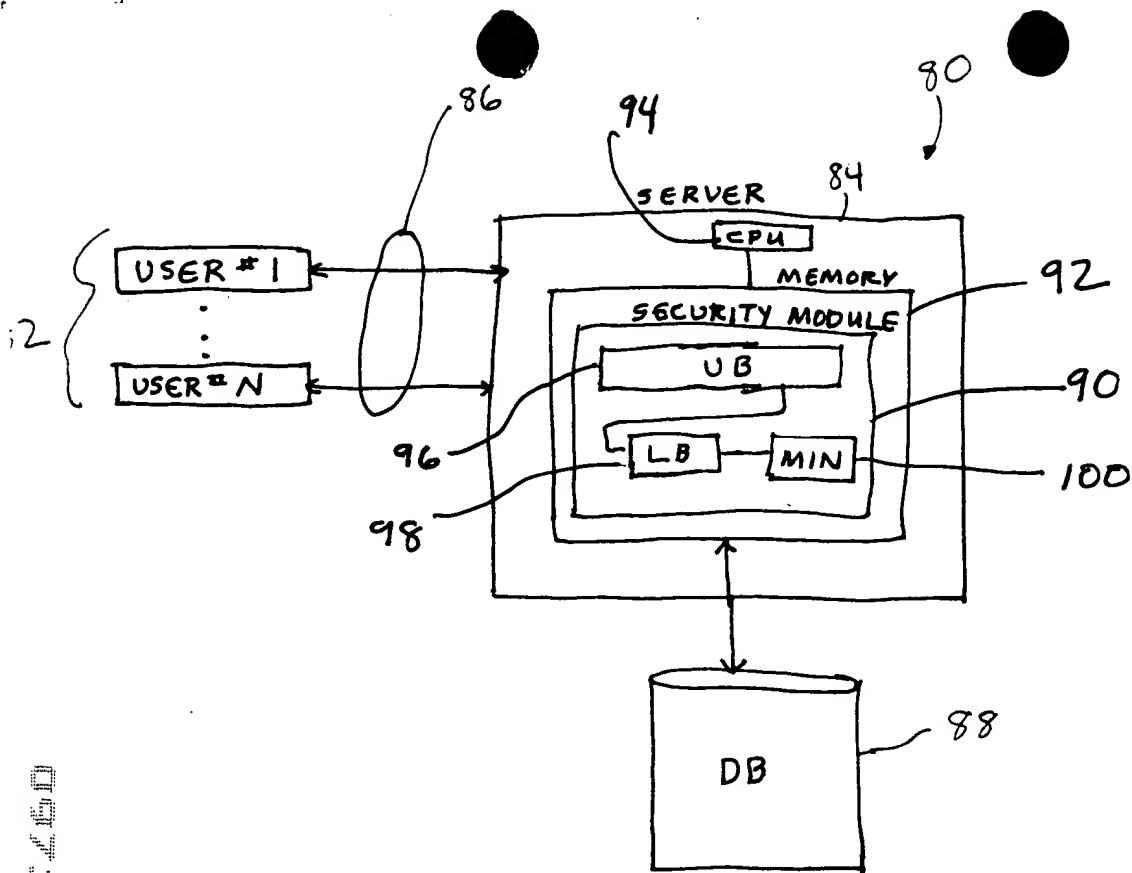


FIGURE 3

$\text{Provider} \succeq \lambda(\text{illness})$
 $\lambda(\text{illness}) \succeq \lambda(\text{division})$
 $\text{lub}\{\lambda(\text{division}), \lambda(\text{plan})\} \succeq \lambda(\text{doctor})$
 $\lambda(\text{illness}) \succeq \text{Research}$
 $\lambda(\text{division}) \succeq \text{Public}$
 $\lambda(\text{plan}) \succeq \text{Financial}$
 $\lambda(\text{doctor}) \succeq \text{Public}$

Figure 5(a)

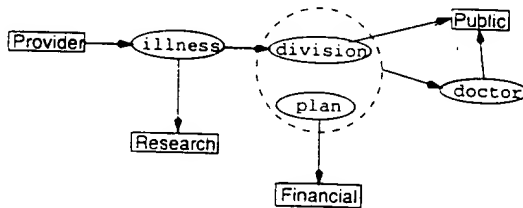


Figure 5(b)

$\lambda(\text{illness}) = \text{Provider}$
 $\lambda(\text{division}) = \text{Provider}$
 $\lambda(\text{plan}) = \text{HMO}$
 $\lambda(\text{doctor}) = \text{HMO}$

Figure 5(c)

0971152.10900

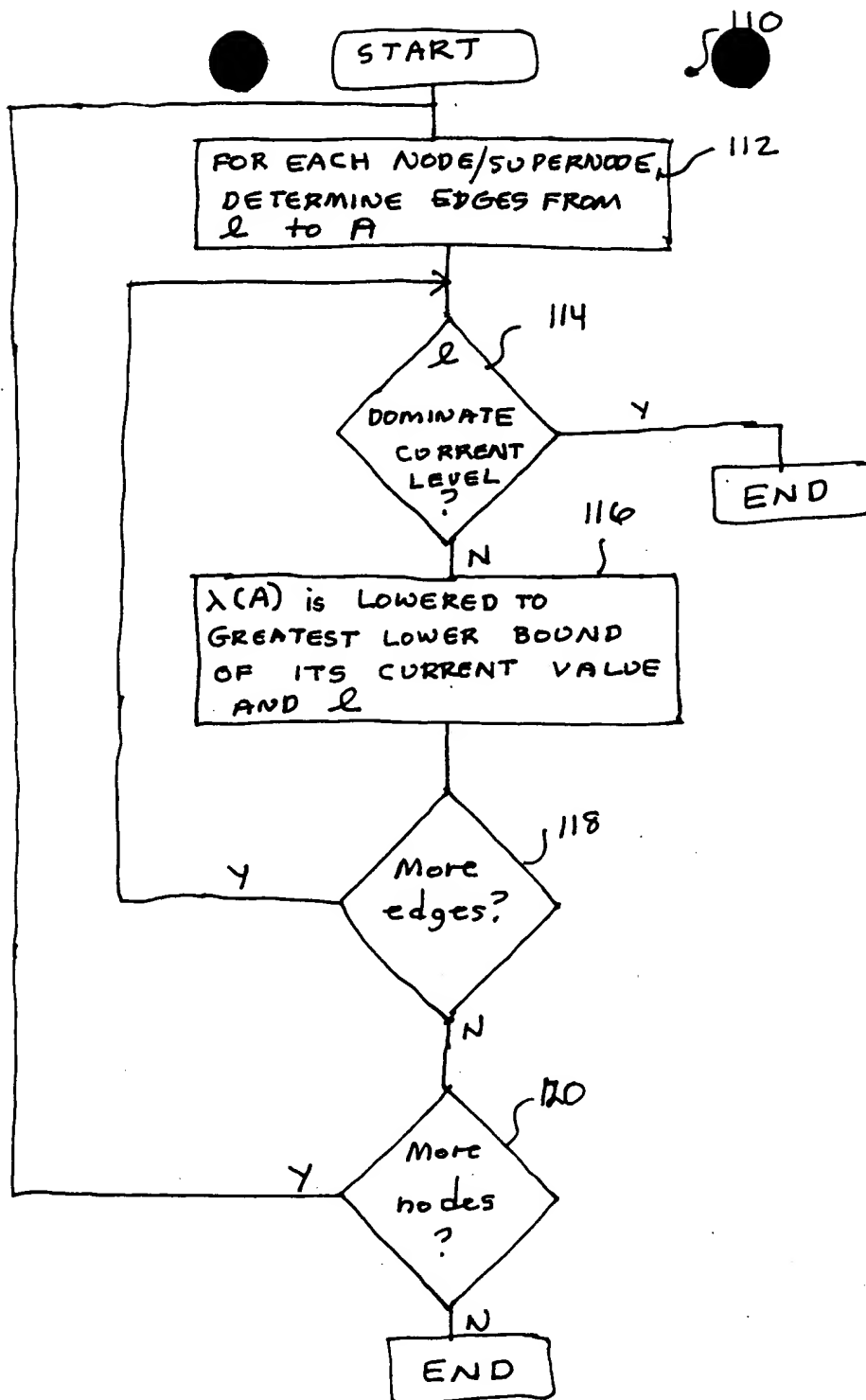


FIGURE 4

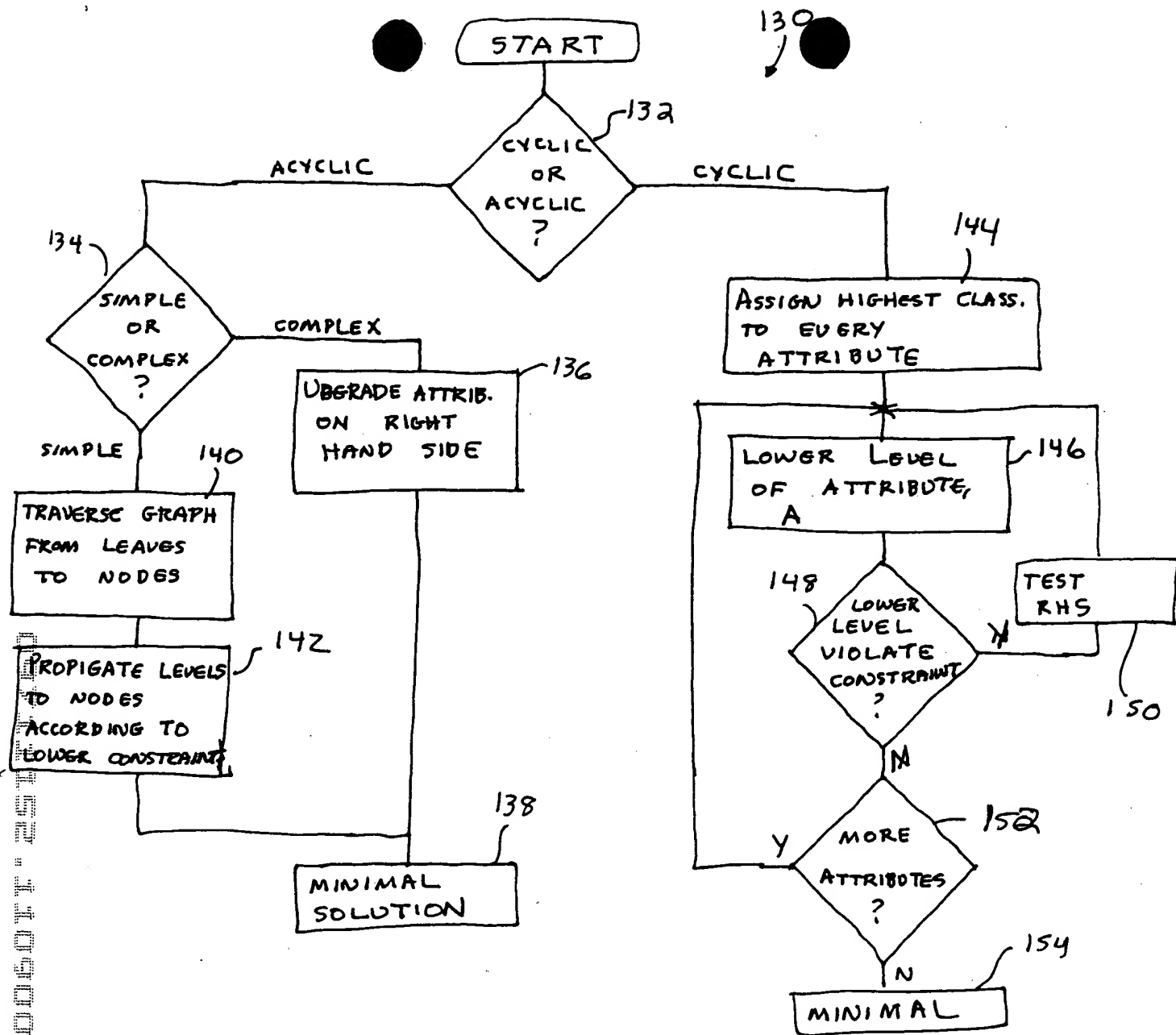


FIGURE 6

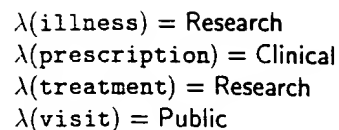


Figure 7 (b)

Figure 7(c)

The diagram shows a dashed oval containing two entities: 'patient' and 'bill'. 'patient' is connected to 'Public' and 'Admin' roles. 'bill' is connected to the 'Financial' role.

$\lambda(\text{bill}) = \text{Financial}$
 $\lambda(\text{patient}) = \text{Research}$

Figure 8 (b)

Figure 8 (c)

Figure 8(d)

```

graph LR
    Public[Public] --> doctor(doctor)
    Public --> division(division)
    doctor --> illness(illness)
    illness --> Research[Research]
    division --> illness
    division --> plan(plan)
    plan --> Financial[Financial]
    subgraph Dashed_Oval [ ]
        doctor
        division
        plan
    end

```

$\lambda(\text{division}) = \text{Public}$
 $\lambda(\text{doctor}) = \text{Research}$
 $\lambda(\text{illness}) = \text{Research}$
 $\lambda(\text{plan}) = \text{Admin}$

Figure 9 (b)

Figure 9(c)

Algorithm 3.1 (Minimal Classification Generation)

```

MAIN
For  $A \in \mathcal{A}$  do  $\text{Constr}[A] := \emptyset$ ;  $\text{visit}[A] := 0$ ;  $\text{done}[A] := \text{FALSE}$ 
For  $l \in L$  do  $\text{done}[l] := \text{TRUE}$ ;  $\text{visit}[l] := 1$ 
For  $c = (lhs, rhs) \in C_{lower}$  do
   $\text{count}[c] := 0$ 
  For  $A \in lhs$  do
     $\text{Constr}[A] := \text{Constr}[A] \cup \{c\}$ ;  $\text{count}[c] := \text{count}[c] + 1$ 
   $\text{Stack} := \emptyset$ 
  For  $A \in \mathcal{A}$  do
    If  $\text{visit}[A] = 0$  then  $\text{dfs\_visit}(A)$ 
   $\text{max\_scc} := 0$ 
  For  $i = 1, \dots, |A|$  do  $\text{scc}[i] := ()$ 
  For  $A \in \mathcal{A}$  do  $\text{visit}[A] := 0$ 
  While NOTEMPTY( $\text{Stack}$ ) do
     $A := \text{POP}(\text{Stack})$ 
    If  $\text{visit}[A] = 0$  then
       $\text{max\_scc} := \text{max\_scc} + 1$ 
       $\text{scc}[\text{max\_scc}] := \langle A \rangle$ 
       $\text{dfs\_back\_visit}(A)$ 
  For  $A \in \mathcal{A}$  do  $\lambda(A) := \top$ ;  $\text{visit}[A] := 0$ 
  compute_upper_bounds
  compute_partial_lubs
  compute_minimal_solution

COMPUTE_UPPER_BOUNDS
For  $(l, A) \in C_{upper}$  do  $\lambda(A) := \lambda(A) \sqcap l$ 
For  $i = 1, \dots, \text{max\_scc}$  do
  For  $A \in \text{scc}[i]$  do
    If  $\text{visit}[A] = 0$  then upper_bound( $A, i$ )

UPPER_BOUND( $A, i$ )
 $\text{visit}[A] := 1$ 
For  $c = (lhs, rhs) \in \text{Constr}[A]$  do
  If  $\text{count}[c] > 0$  then  $\text{count}[c] := \text{count}[c] - 1$ 
  If  $\text{count}[c] = 0$  or  $rhs \in \text{scc}[i]$  then
     $\text{levlhs} := \perp$ 
    For  $A' \in lhs$  do  $\text{levlhs} := \text{levlhs} \sqcup \lambda(A')$ 
    If  $\neg(\text{levlhs} \geq \lambda(rhs))$  then
      If  $rhs \in L$  then Fail
      else  $\lambda(rhs) := \lambda(rhs) \sqcap \text{levlhs}$ 
      If  $rhs \in \text{scc}[i]$  then
        upper_bound( $rhs, i$ )

COMPUTE_MINIMAL_SOLUTION
For  $i := \text{max\_scc}, \dots, 1$  do
  For  $A \in \text{scc}[i]$  do
     $\text{done}[A] := \text{TRUE}$ ;  $l := \perp$ 
    For  $c = (lhs, rhs) \in \text{Constr}[A]$  do
      If  $\text{done}[rhs]$  then
        case  $|lhs|$  of
          1:  $l := l \sqcup \lambda(rhs)$ 
          >1:  $l := l \sqcup \text{minlevel}(A, c)$ 
      else  $\text{done}[A] := \text{FALSE}$ 
    If  $\text{done}[A]$  then  $\lambda(A) := l$ 
  else  $DSet := \{l' \mid l' \text{ is a maximal level, } \lambda(A) \succ l' \geq l\}$ 
  While  $DSet \neq \emptyset$ 
    Choose  $l''$  in  $DSet$ ;  $DSet := DSet - l''$ 
     $\text{Lower} := \text{try\_to\_lower}(A, l'')$ 
    If  $\text{Lower} \neq \emptyset$  then
      For  $(A', l') \in \text{Lower}$  do  $\lambda(A') := l'$ 
       $DSet := \{l' \mid l' \text{ maximal level, } \lambda(A) \succ l' \geq l\}$ 
     $\text{done}[A] := \text{TRUE}$ 
  For  $c \in \text{Constr}[A]$  do
     $j := \text{count}[c]$ ;  $\text{Plub}[c][j] := \lambda(A) \sqcup \text{Plub}[c][j+1]$ 
     $\text{count}[c] := \text{count}[c] - 1$ 

DFS_VISIT( $A$ )
 $\text{visit}[A] := 1$ 
For  $(lhs, rhs) \in \text{Constr}[A]$  do
  If  $\text{visit}[rhs] = 0$  then  $\text{dfs\_visit}(rhs)$ 
  PUSH( $A, \text{Stack}$ )

DFS_BACK_VISIT( $A$ )
/* Traverses the constraints backward and inserts all
attributes found in the same SCC list as  $A$  */
 $\text{visit}[A] := 1$ 
For  $(lhs, A) \in C_{lower}$  do
  For  $A' \in lhs$  do
    If  $\text{visit}[A'] = 0$  then
       $\text{scc}[\text{max\_scc}] := \text{concat}(\langle A' \rangle, \text{scc}[\text{max\_scc}])$ 
       $\text{dfs\_back\_visit}(A')$ 

COMPUTE_PARTIAL_LUBS
For  $c = (lhs, rhs) \in C_{lower}$  do  $\text{count}[c] := 0$ ;  $\text{Plub}[c][0] := \perp$ 
For  $i = 1, \dots, \text{max\_scc}$  do
  For  $A \in \text{reverse}(\text{scc}[i])$  do
    For  $c = (lhs, rhs) \in \text{Constr}[A]$  do
       $\text{count}[c] := \text{count}[c] + 1$ ;  $j := \text{count}[c]$ 
       $\text{Plub}[c][j] := \text{Plub}[c][j-1] \sqcup \lambda(A)$ 
  For  $c = (lhs, rhs) \in C_{lower}$  do  $j := \text{count}[c] + 1$ ;  $\text{Plub}[c][j] := \perp$ 

MINLEVEL( $A, c$ )
/* Returns a minimal level for  $A$  that keeps  $c$  satisfied */
 $j := \text{count}[c]$ ;  $(lhs, rhs) := c$ ;  $\text{last} := \lambda(A)$ 
 $\text{lubothers} := \text{Plub}[c][j-1] \sqcup \text{Plub}[c][j+1]$ 
If  $\text{lubothers} \geq \lambda(rhs)$  then  $\text{last} := \perp$ 
else Try :=  $\{l \mid l \text{ is a maximal level s. t. } \text{last} > l\}$ 
While Try  $\neq \emptyset$  do
  Choose  $l$  in Try; Try := Try -  $l$ 
  if  $(l \sqcup \text{lubothers}) \geq \lambda(rhs)$  then
     $\text{last} := l$ ; Try :=  $\{l \mid l \text{ is a maximal level s. t. } \text{last} > l\}$ 
return last

TRY_TO_LOWER( $A, l$ )
Tocheck :=  $\{(A, l)\}$ 
Tolower :=  $\emptyset$ 
Repeat
  Choose  $(A', l') \in \text{Tocheck}$ 
  Tocheck := Tocheck -  $\{(A', l')\}$ 
  Tolower := Tolower  $\cup \{(A', l')\}$ 
  For  $(lhs, rhs) \in \text{Constr}[A']$  do
    level :=  $\perp$ 
    For  $A'' \in lhs$  do
      If  $\exists (A'', l'') \in \text{Tolower}$  then
        level := level  $\sqcup l''$ 
      else level := level  $\sqcup \lambda(A'')$ 
    case  $\text{done}[rhs]$  of
      TRUE: If  $\neg(\text{level} \geq \lambda(rhs))$  then return  $\emptyset$ 
      FALSE: If  $\neg(\text{level} \geq \lambda(rhs))$  then
        newlevel :=  $\lambda(rhs) \sqcap \text{level}$ 
        If  $\exists (rhs, l'') \in (\text{Tolower} \cup \text{Tocheck})$  then
          If  $\neg(\text{newlevel} \geq l'')$  then
            newlevel :=  $l'' \sqcap \text{newlevel}$ 
          If  $(rhs, l'') \in \text{Tolower}$  then
            Tolower := Tolower -  $\{(rhs, l'')\}$ 
          else Tocheck := Tocheck -  $\{(rhs, l'')\}$ 
          Tocheck := Tocheck  $\cup \{(rhs, \text{newlevel})\}$ 
        else Tocheck := Tocheck  $\cup \{(rhs, \text{newlevel})\}$ 
until Tocheck =  $\emptyset$ 
return Tolower

```

Figure 10 Algorithm for computing a minimal classification.

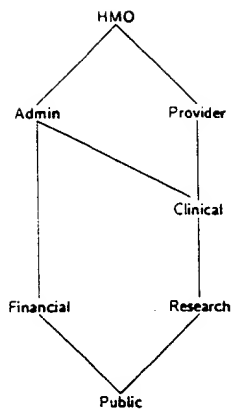


Figure 11 (a)

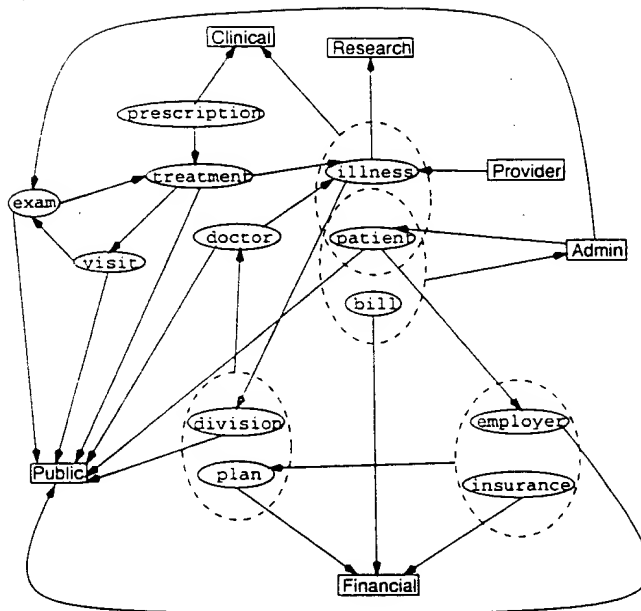


Figure 11 (b)

		SCC											
		[8]	[7]	[6]	[5]	[4]	[3]	[2]		[1]			
		doctor	division	illness	plan	employer	patient	bill	insurance	exam	treatment	visit	prescription
• initial levels		HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO
doctor	compute_upper_bounds	HMO	Clinical	Clinical	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(doctor,Admin) F	Admin	Clinical	Clinical	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(doctor,Financial)	Admin	Clinical	Clinical	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(doctor,Clinical)	Clinical	Clinical	Clinical	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(doctor,Research)	Research	Research	Research	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
division	try_to_lower(doctor,Public) F	Research	Research	Research	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	-		Public	Research	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	-			Research	HMO	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	-				Admin	Admin	Admin	HMO	HMO	Admin	Admin	Admin	HMO
	-					Public	Admin	HMO	HMO	Admin	Admin	Admin	HMO
illness	-						Clinical	HMO	HMO	Admin	Admin	Admin	HMO
	-							Financial	Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
employer	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
patient	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
bill	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
insurance	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
	-								Admin	Admin	Admin	Admin	HMO
exam	try_to_lower(exam,Financial) F								Admin	Admin	Admin	Admin	HMO
	try_to_lower(exam,Clinical)								Clinical	Clinical	Clinical	Clinical	HMO
	try_to_lower(exam,Research)								Research	Research	Research	Research	HMO
	try_to_lower(exam,Public) F								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
treatment	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
visit	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
prescription	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
	-								Research	Research	Research	Research	HMO
• final levels		Research	Public	Research	Admin	Public	Clinical	Financial	Admin	Research	Research	Research	Clinical

Figure 11 (c)

SCC

		[8]	[7]	[6]	[5]	[4]	[3]	[2]	[1]				
* initial levels		doctor	division	illness	plan	employer	patient	bill	insurance	exam	treatment	visit	prescription
patient	compute_upper_bounds	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO	HMO
	try_to_lower(patient,Financial)	HMO	Clinical	Clinical	HMO	Financial	Financial	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(patient,Public)	HMO	Clinical	Clinical	HMO	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(plan,Admin)	Admin	Clinical	Clinical	Admin	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
plan	try_to_lower(plan,Financial)	Admin	Clinical	Clinical	Financial	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(doctor,Financial)F	Admin	Clinical	Clinical	Financial	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
doctor	try_to_lower(doctor,Clinical)	Clinical	Clinical	Clinical	Financial	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
	try_to_lower(doctor,Research)F	Clinical	Clinical	Clinical	Financial	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
division	-	Clinical	Research	Clinical	Financial	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
illness	-				Financial	Public	Public	HMO	HMO	Admin	Admin	Admin	HMO
employer	-					Public		HMO	HMO	Admin	Admin	Admin	HMO
bill	-							Admin	HMO	Admin	Admin	Admin	HMO
insurance	-								Financial	Admin	Admin	Admin	HMO
exam	try_to_lower(exam,Financial)F									Admin	Admin	Admin	HMO
	try_to_lower(exam,Clinical)									Clinical	Clinical	Clinical	HMO
	try_to_lower(exam,Research)F									Clinical	Clinical	Clinical	HMO
treatment	try_to_lower(treatment,Clinical)									Clinical	Clinical	Clinical	HMO
visit	-											Clinical	HMO
prescription	-												Clinical
* final levels		Clinical	Research	Clinical	Financial	Public	Public	Admin	Financial	Clinical	Clinical	Clinical	Clinical

Figure 12

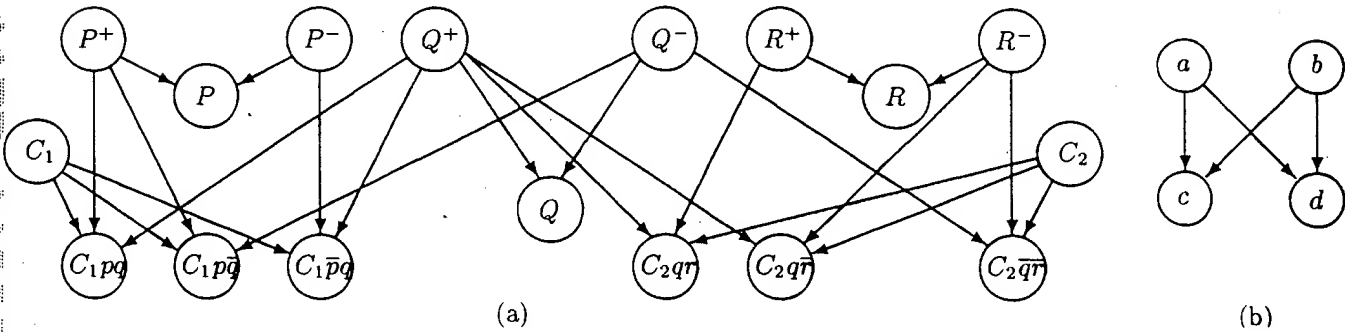


Figure 13 A + B

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